



General Certificate of Education

Mathematics 6300

Specification A

MAD1 Discrete 1

Mark Scheme

2005 examination – June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Key to Mark Scheme

M	mark is for	method
m	mark is dependent on one or more M marks and is for	method
A	mark is dependent on M or m marks and is for	accuracy
B	mark is independent of M or m marks and is for	accuracy
E	mark is for	explanation
√ or ft or F		follow through from previous incorrect result
CAO		correct answer only
AWFW		anything which falls within
AWRT		anything which rounds to
AG		answer given
SC		special case
OE		or equivalent
A2,1		2 or 1 (or 0) accuracy marks
-x EE		deduct x marks for each error
NMS		no method shown
PI		possibly implied
SCA		substantially correct approach
c		candidate
sf		significant figure(s)
dp		decimal place(s)

Abbreviations used in Marking

MC – x	deducted x marks for mis-copy
MR – x	deducted x marks for mis-read
ISW	ignored subsequent working
BOD	given benefit of doubt
WR	work replaced by candidate
FB	formulae book

Application of Mark Scheme

No method shown:

Correct answer without working	mark as in scheme
Incorrect answer without working	zero marks unless specified otherwise

More than one method / choice of solution:

2 or more complete attempts, neither/none crossed out	mark both/all fully and award the mean mark rounded down
1 complete and 1 partial attempt, neither crossed out	award credit for the complete solution only

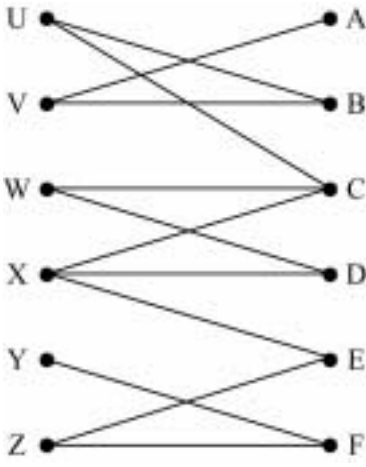
Crossed out work

do not mark unless it has not been replaced

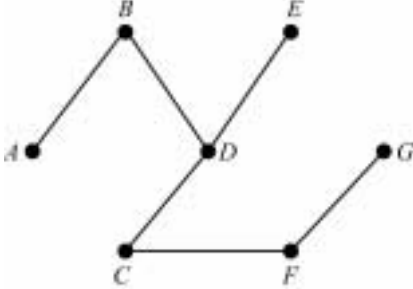
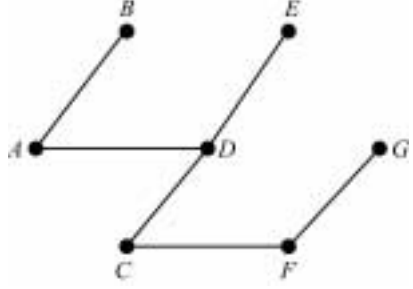
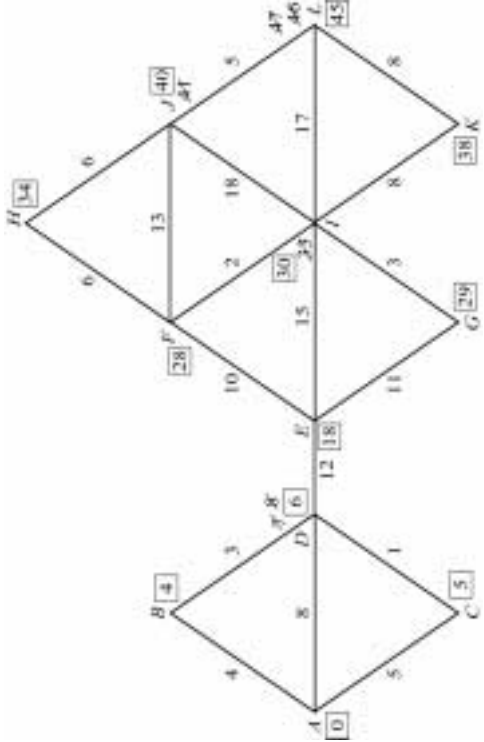
Alternative solution using a correct or partially correct method

award method and accuracy marks as appropriate

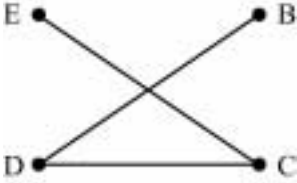
MAD1

Q	Solution	Marks	Total	Comments
1		M1		bipartite graph
(b)	Initial BV, CU, DX, FZ $A \rightarrow V$ $B \rightarrow U$ $C \rightarrow W$ $E \rightarrow Z$ $F \rightarrow Y$ Match: AV, BU, CW, DX, EZ, FY (CX, DW)	M1A1 M1A1 B1	2 5	starting with A, W starting with E, Y } Either Order Or: $E \rightarrow X \rightarrow D \rightarrow W$ $A \rightarrow V \rightarrow B \rightarrow U \rightarrow C \rightarrow W \rightarrow D \rightarrow X$
Total			7	
2(a)	23 12 17 18 5 9 19 16 5 23 9 12 17 19 16 18 5 9 17 16 23 12 19 18 5 17 19 23 9 12 16 18 5 9 17 12 19 16 23 18 5 9 12 16 17 18 19 23	M1 M1 A1 M1 A1 A1		SCA 4 sublists 2 sublists all correct
(b)(i)	Comparisons = 4	B1	1	
(ii)	Swaps = 3	B1	1	
Total			8	

MAD1 (cont)

Q	Solution	Marks	Total	Comments
3(a)	$AB = 3$ $FG = 4$ $ED = 5$ $FC = 6$ $BD = 7$ or $AD = 7$ $CD = 9$	M1	4	SCA
		A1		FG second
		B1		6 edges
(b)	Length = 34	A1	1	all correct
(c)		B1	2	
B1F				
Total			7	
4(a)(i)		M1	6	SCA
		A1		3 values at <i>D</i>
		M1		2 values at <i>I</i>
		M1		3 values at <i>L</i>
		A1		all correct
		B1		45 at <i>L</i>
(ii)	$ACDEFHJL$	B1	1	
(b)(i)	Odd vertices at <i>A</i> and <i>L</i> Total (155) (+ their 45) = 200	M1	3	CAO
		M1		
(ii)	Order of $F = 4 + 2 = 6$ $\therefore F$ appears 3 times	A1	1	
Total			11	

MAD1 (cont)

Q	Solution	Marks	Total	Comments
5(a)	A B C D E A 7 8 5 10 3 = 33	B1	1	
(b)	Tour; may be improved	E1E1	2	
(c)	A → E → C → D → B → A 3 4 5 6 7 = 25	M1 M1 A1 B1	4	tour visits all vertices correct order
(d)	MST  = 4 + 5 + 6 = 15 Add 3 + 7 15 + 10 = 25	M1 A1 M1 A1	4	MST with 3 edges or 15 + 2 × 3 = 21
(e)	Cannot be lower than a lower bound	E1	1	
Total			12	

MAD1 (cont)

Q	Solution	Marks	Total	Comments
6(a)	$y \geq \frac{1}{2}x \Rightarrow 2y \geq x$	B1	2	
	$20x + 10y \leq 600$ so $2x + y \leq 60$	B1		
(b)	$x \geq 5, y \geq 5, y \leq 25$	B1	2	all correct
	$P = 3x + y$	B1		
(c)		B1 × 2	5	diagonal lines $x \geq 5, y \geq 5, y \leq 25$
		B1		
(d)	Max at $x = 24, y = 12$ $P = 84$	B1	2	feasible region
		A1		
(e)	$P = 2x + 2y$ Max at $(17.5, 25)$ Not integers Values $(17, 25)$ and $(18, 24)$ give $P = 510$ (6 hrs) + 84 (1hr) = £594	M1	4	objective line
		B1, B1		
		A1	4	CAO
	Total		15	
	TOTAL		60	