

General Certificate of Education
January 2005
Advanced Level Examination



MATHEMATICS (SPECIFICATION A)
Unit Mechanics 2

MAM2/W

Tuesday 25 January 2005 Morning Session

In addition to this paper you will require:

- an 8-page answer book;
- the AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed: 1 hour 20 minutes

Instructions

- Use blue or black ink or ball-point pen. Pencil should only be used for drawing.
- Write the information required on the front of your answer book. The *Examining Body* for this paper is AQA. The *Paper Reference* is MAM2/W.
- Answer **all** questions.
- Take $g = 9.8 \text{ m s}^{-2}$ unless otherwise stated.
- All necessary working should be shown; otherwise marks for method may be lost.
- The **final** answer to questions requiring the use of tables or calculators should normally be given to three significant figures.
- Tie loosely any additional sheets you have used to the back of your answer book before handing it to the invigilator.

Information

- The maximum mark for this paper is 60.
- Mark allocations are shown in brackets.

Advice

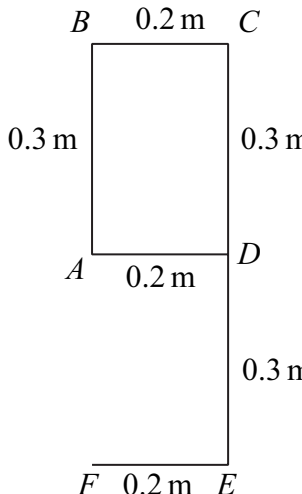
- Unless stated otherwise, formulae may be quoted, without proof, from the booklet.

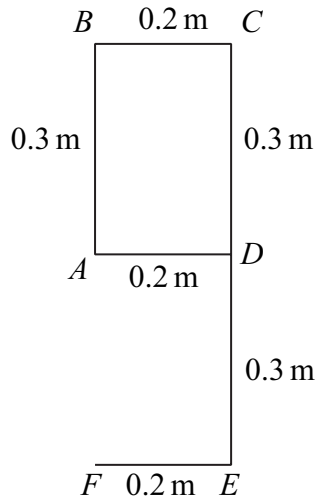
Answer **all** questions.

1 A particle of mass 2 kg is moving under the action of a single force, \mathbf{F} newtons.

(a) Calculate the kinetic energy of the particle when its velocity is $3\mathbf{i} + 4\mathbf{j} \text{ m s}^{-1}$.
(2 marks)

(b) Given that $\mathbf{F} = 6\mathbf{i} - \mathbf{j}$, find the power of the force when the velocity of the particle is $3\mathbf{i} + 4\mathbf{j} \text{ m s}^{-1}$.
(2 marks)

2 As part of an advertising display, a thin uniform rod of length 1.5 m is bent to form a figure . The diagram shows the figure in which $ABCD$ is a rectangle and angle $ADE = \text{angle } DEF = 90^\circ$.



(a) The mass of BC is $2M$.

Express the total mass of the figure as a multiple of M .
(1 mark)

(b) (i) Show that the centre of mass of the figure is at a distance of 0.27 m from BC .
(4 marks)

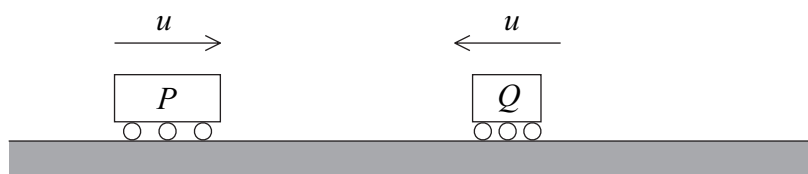
(ii) Find the distance of the centre of mass of the figure from CE .
(3 marks)

(c) When freely suspended from the point C , the side CE of the figure makes an angle θ with the vertical.

Determine the value of θ , giving your answer in degrees to one decimal place.

(3 marks)

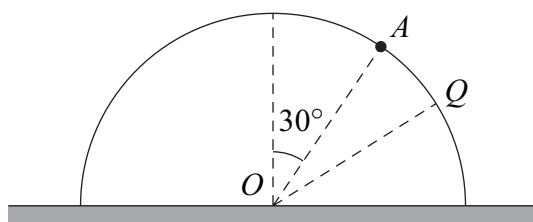
- 3 Alina, who has mass 50 kg, is attached to one end of an elastic cord. The cord has natural length 20 metres and stiffness $k \text{ N m}^{-1}$. The other end of the cord is attached to a bridge. Alina steps off the bridge at the point where the cord is attached and falls vertically. Throughout the subsequent motion, Alina can be modelled as a particle.
- (a) Find Alina's speed when she passes through the point 20 metres vertically below the bridge. (2 marks)
- (b) The cord stretches to a total length of 32 metres before Alina comes momentarily to rest.
- (i) Show that the elastic potential energy of the cord at the instant when she is momentarily at rest is 15 680 J. (2 marks)
- (ii) Hence find the stiffness of the cord. (3 marks)
- 4 Two toy train carriages, P and Q , have masses $2m$ and m respectively. They are moving directly towards each other, as shown in the diagram. Both carriages have speed u .



The carriages collide and subsequently Q moves in the same direction as P . The coefficient of restitution between P and Q is e .

- (a) (i) Show that the speed of carriage P immediately after the collision is $\frac{u}{3}(1 - 2e)$ and find the speed of carriage Q . (7 marks)
- (ii) Deduce that $e < \frac{1}{2}$. (2 marks)
- (b) The magnitude of the impulse on P due to the collision is I . Show that:
- (i) $I = \frac{4mu}{3}(1 + e)$; (3 marks)
- (ii) $\frac{4mu}{3} \leq I < 2mu$. (2 marks)

- 5 A solid smooth hemisphere, of radius r , has its plane face fixed to a horizontal table. The centre of the plane face is O .



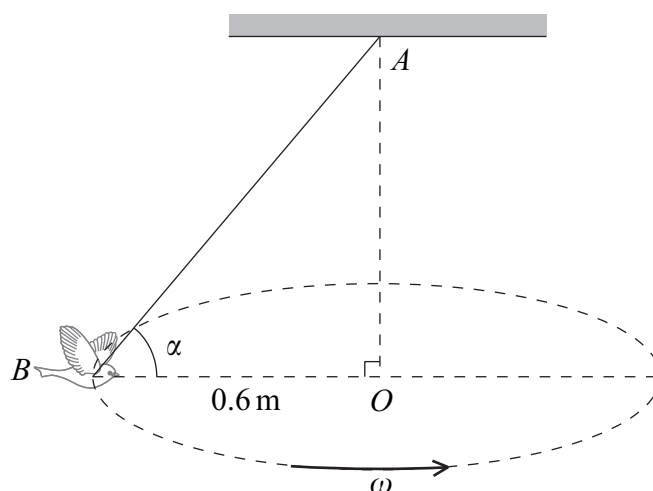
A particle P , of mass m , is released from rest at a point A on the surface of the hemisphere, where OA makes an angle of 30° with the upward vertical through O . The particle P slides freely down the surface. At the point Q on the surface, the particle has speed v and OQ makes an angle θ with the upward vertical through O .

- (a) Show that $v^2 = gr(\sqrt{3} - 2 \cos \theta)$. (4 marks)
- (b) Find, in terms of m , g and θ , an expression for the reaction force of the hemisphere on the particle at the point Q . (5 marks)
- (c) When $\theta = \alpha$, the particle loses contact with the hemisphere.

Find the value of α , giving your answer to the nearest degree. (2 marks)

- 6 A toy bird, of mass 0.25 kg, is fixed to one end, B , of a light inextensible string. The other end, A , of the string is attached to a fixed point on a ceiling. The bird is set in motion, so that it describes a horizontal circle of radius 0.6 m. The centre of this circle is O , which is vertically below A , as shown in the diagram. The angle ABO is α .

The bird moves with a constant angular speed of ω radians per second.



The bird completes one full revolution every 1.5 seconds.

- (a) Find ω , leaving your answer in terms of π . *(2 marks)*
- (b) (i) Determine the magnitude of the acceleration of the bird. *(2 marks)*
(ii) Show the direction of this acceleration on a diagram. *(1 mark)*
- (c) (i) Draw a diagram to show the forces acting on the bird. *(1 mark)*
(ii) Find the angle α , giving your answer to the nearest degree. *(6 marks)*
- (d) State **one** modelling assumption used in this question. *(1 mark)*

END OF QUESTIONS

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