

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
TOTAL	



General Certificate of Education
Advanced Level Examination
June 2014

Mathematics

MPC4

Unit Pure Core 4

Thursday 12 June 2014 1.30 pm to 3.00 pm

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



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4 A painting was valued on 1 April 2001 at £5000 .

The value of this painting is modelled by

$$V = Ap^t$$

where £ V is the value t years after 1 April 2001, and A and p are constants.

(a) Write down the value of A .

[1 mark]

(b) According to the model, the value of this painting on 1 April 2011 was £25 000 .

Using this model:

(i) show that $p^{10} = 5$;

[1 mark]

(ii) use logarithms to find the year in which the painting will be valued at £75 000 .

[4 marks]

(c) A painting by another artist was valued at £2500 on 1 April 1991. The value of this painting is modelled by

$$W = 2500q^t$$

where £ W is the value t years after 1 April 1991, and q is a constant.

(i) Show that, according to the two models, the value of the two paintings will be the same T years after 1 April 1991,

$$\text{where } T = \frac{\ln\left(\frac{5}{2}\right)}{\ln\left(\frac{p}{q}\right)}$$

[4 marks]

(ii) Given that $p = 1.029q$, find the year in which the two paintings will have the same value.

[1 mark]

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6 The line l_1 has equation $\mathbf{r} = \begin{bmatrix} 4 \\ -5 \\ 3 \end{bmatrix} + \lambda \begin{bmatrix} -1 \\ 3 \\ 1 \end{bmatrix}$.

The line l_2 has equation $\mathbf{r} = \begin{bmatrix} 7 \\ -8 \\ 6 \end{bmatrix} + \mu \begin{bmatrix} 2 \\ -3 \\ 1 \end{bmatrix}$.

The point P lies on l_1 where $\lambda = -1$. The point Q lies on l_2 where $\mu = 2$.

(a) Show that the vector \overrightarrow{PQ} is parallel to $\begin{bmatrix} 1 \\ -1 \\ 1 \end{bmatrix}$.

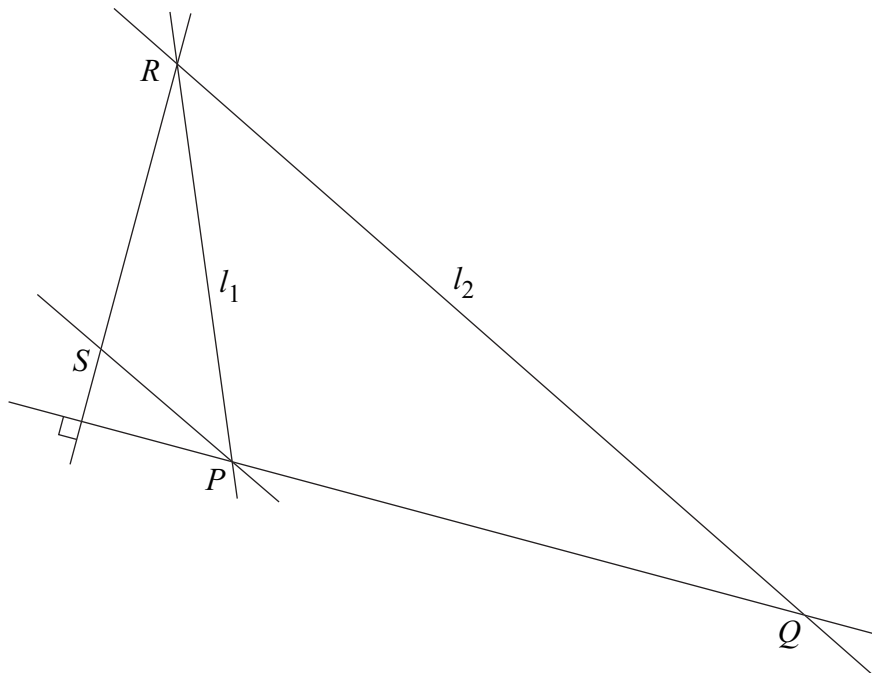
[3 marks]

(b) The lines l_1 and l_2 intersect at the point $R(3, b, c)$.

(i) Show that $b = -2$ and find the value of c .

[3 marks]

(ii) The point S lies on a line through P that is parallel to l_2 . The line RS is perpendicular to the line PQ .



Find the coordinates of S .

[4 marks]



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7 A curve has equation $\cos 2y + ye^{3x} = 2\pi$.

The point $A\left(\ln 2, \frac{\pi}{4}\right)$ lies on this curve.

(a) (i) Find an expression for $\frac{dy}{dx}$.

[6 marks]

(ii) Hence find the exact value of the gradient of the curve at A .

[1 mark]

(b) The normal at A crosses the y -axis at the point B . Find the exact value of the y -coordinate of B .

[2 marks]

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