

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
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TOTAL	



General Certificate of Education
Advanced Level Examination
June 2010

Mathematics

MFP4

Unit Further Pure 4

Tuesday 15 June 2010 9.00 am to 10.30 am

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.



J U N 1 0 M F P 4 0 1

Answer **all** questions in the spaces provided.

1 The position vectors of the points P , Q and R are, respectively,

$$\mathbf{p} = \begin{bmatrix} 3 \\ 4 \\ -1 \end{bmatrix}, \quad \mathbf{q} = \begin{bmatrix} -1 \\ 2 \\ 2 \end{bmatrix} \quad \text{and} \quad \mathbf{r} = \begin{bmatrix} 1 \\ 4 \\ 1 \end{bmatrix}$$

(a) Show that \mathbf{p} , \mathbf{q} and \mathbf{r} are linearly dependent. (2 marks)

(b) Determine the area of triangle PQR . (4 marks)

QUESTION
PART
REFERENCE



2 Let $\mathbf{A} = \begin{bmatrix} 1 & x \\ 2 & 3 \end{bmatrix}$, $\mathbf{B} = \begin{bmatrix} 1 & -1 \\ 2 & 2 \end{bmatrix}$ and $\mathbf{C} = \begin{bmatrix} 4 - 4x & 8 \\ 8x - 4 & 4 \end{bmatrix}$.

(a) Find \mathbf{AB} in terms of x . (2 marks)

(b) Show that $\mathbf{B}^T \mathbf{A}^T = \mathbf{C}$ for some value of x . (5 marks)

QUESTION
PART
REFERENCE



4 The fixed points A and B and the variable point C have position vectors

$$\mathbf{a} = \begin{bmatrix} 3 \\ -4 \\ 1 \end{bmatrix}, \quad \mathbf{b} = \begin{bmatrix} 2 \\ 1 \\ -3 \end{bmatrix} \quad \text{and} \quad \mathbf{c} = \begin{bmatrix} 2-t \\ t \\ 5 \end{bmatrix}$$

respectively, relative to the origin O , where t is a scalar parameter.

- (a) Find an equation of the line AB in the form $(\mathbf{r} - \mathbf{u}) \times \mathbf{v} = \mathbf{0}$. (3 marks)
- (b) Determine $\mathbf{b} \times \mathbf{c}$ in terms of t . (4 marks)
- (c) (i) Show that $\mathbf{a} \cdot (\mathbf{b} \times \mathbf{c})$ is constant for all values of t , and state the value of this constant. (2 marks)
- (ii) Write down a geometrical conclusion that can be deduced from the answer to part (c)(i). (1 mark)

QUESTION
PART
REFERENCE



5

Factorise fully the determinant

$$\begin{vmatrix} x & y & z \\ x^2 & y^2 & z^2 \\ yz & zx & xy \end{vmatrix}.$$

(8 marks)

QUESTION
PART
REFERENCE

Area for writing the answer, consisting of horizontal dotted lines.



6 The line L and the plane Π have vector equations

$$\mathbf{r} = \begin{bmatrix} 7 \\ 8 \\ 50 \end{bmatrix} + t \begin{bmatrix} 6 \\ 2 \\ -9 \end{bmatrix} \quad \text{and} \quad \mathbf{r} = \begin{bmatrix} -2 \\ 0 \\ -25 \end{bmatrix} + \lambda \begin{bmatrix} 5 \\ 3 \\ 4 \end{bmatrix} + \mu \begin{bmatrix} 1 \\ 6 \\ 2 \end{bmatrix}$$

respectively.

(a) (i) Find direction cosines for L . (2 marks)

(ii) Show that L is perpendicular to Π . (3 marks)

(b) For the system of equations

$$\begin{aligned} 6p + 5q + r &= 9 \\ 2p + 3q + 6r &= 8 \\ -9p + 4q + 2r &= 75 \end{aligned}$$

form a pair of equations in p and q only, and hence find the unique solution of this system of equations. (5 marks)

(c) It is given that L meets Π at the point P .

(i) Demonstrate how the coordinates of P may be obtained from the system of equations in part **(b)**. (2 marks)

(ii) Hence determine the coordinates of P . (2 marks)

QUESTION
PART
REFERENCE



There are no questions printed on this page

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ANSWER IN THE SPACES PROVIDED**

