

Centre Number						Candidate Number				
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Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
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5	
6	
7	
8	
9	
TOTAL	



General Certificate of Education
Advanced Subsidiary Examination
June 2014

Mathematics

MFP1

Unit Further Pure 1

Tuesday 10 June 2014 9.00 am to 10.30 am

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



J U N 1 4 M F P 1 0 1

Answer **all** questions.

Answer each question in the space provided for that question.

1 A curve passes through the point (9, 6) and satisfies the differential equation

$$\frac{dy}{dx} = \frac{1}{2 + \sqrt{x}}$$

Use a step-by-step method with a step length of 0.25 to estimate the value of y at $x = 9.5$. Give your answer to four decimal places.

[5 marks]

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2 The quadratic equation

$$2x^2 + 8x + 1 = 0$$

has roots α and β .

(a) Write down the value of $\alpha + \beta$ and the value of $\alpha\beta$.

[2 marks]

(b) (i) Find the value of $\alpha^2 + \beta^2$.

[2 marks]

(ii) Hence, or otherwise, show that $\alpha^4 + \beta^4 = \frac{449}{2}$.

[2 marks]

(c) Find a quadratic equation, with integer coefficients, which has roots

$$2\alpha^4 + \frac{1}{\beta^2} \text{ and } 2\beta^4 + \frac{1}{\alpha^2}$$

[5 marks]

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4 Find the complex number z such that

$$5iz + 3z^* + 16 = 8i$$

Give your answer in the form $a + bi$, where a and b are real.

[6 marks]

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9 An ellipse E has equation

$$\frac{x^2}{16} + \frac{y^2}{9} = 1$$

- (a) Sketch the ellipse E , showing the values of the intercepts on the coordinate axes. **[2 marks]**
- (b) Given that the line with equation $y = x + k$ intersects the ellipse E at two distinct points, show that $-5 < k < 5$. **[5 marks]**
- (c) The ellipse E is translated by the vector $\begin{bmatrix} a \\ b \end{bmatrix}$ to form another ellipse whose equation is $9x^2 + 16y^2 + 18x - 64y = c$. Find the values of the constants a , b and c . **[5 marks]**
- (d) **Hence** find an equation for each of the two tangents to the ellipse $9x^2 + 16y^2 + 18x - 64y = c$ that are parallel to the line $y = x$. **[3 marks]**

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END OF QUESTIONS



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ANSWER IN THE SPACES PROVIDED**

