

| | | | | | | | | | | |
|---------------------|--|--|--|--|--|------------------|--|--|--|--|
| Centre Number | | | | | | Candidate Number | | | | |
| Surname | | | | | | | | | | |
| Other Names | | | | | | | | | | |
| Candidate Signature | | | | | | | | | | |

| | |
|---------------------|------|
| For Examiner's Use | |
| Examiner's Initials | |
| Question | Mark |
| 1 | |
| 2 | |
| 3 | |
| 4 | |
| 5 | |
| 6 | |
| 7 | |
| 8 | |
| 9 | |
| 10 | |
| TOTAL | |



General Certificate of Education
Advanced Level Examination
June 2013

Mathematics

MPC3

Unit Pure Core 3

Thursday 6 June 2013 9.00 am to 10.30 am

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



J U N 1 3 M P C 3 0 1

QUESTION
PART
REFERENCE

Answer space for question 1

A large rectangular area with horizontal dotted lines for writing an answer.



QUESTION
PART
REFERENCE

Answer space for question 2

A large rectangular area with horizontal dotted lines for writing an answer.



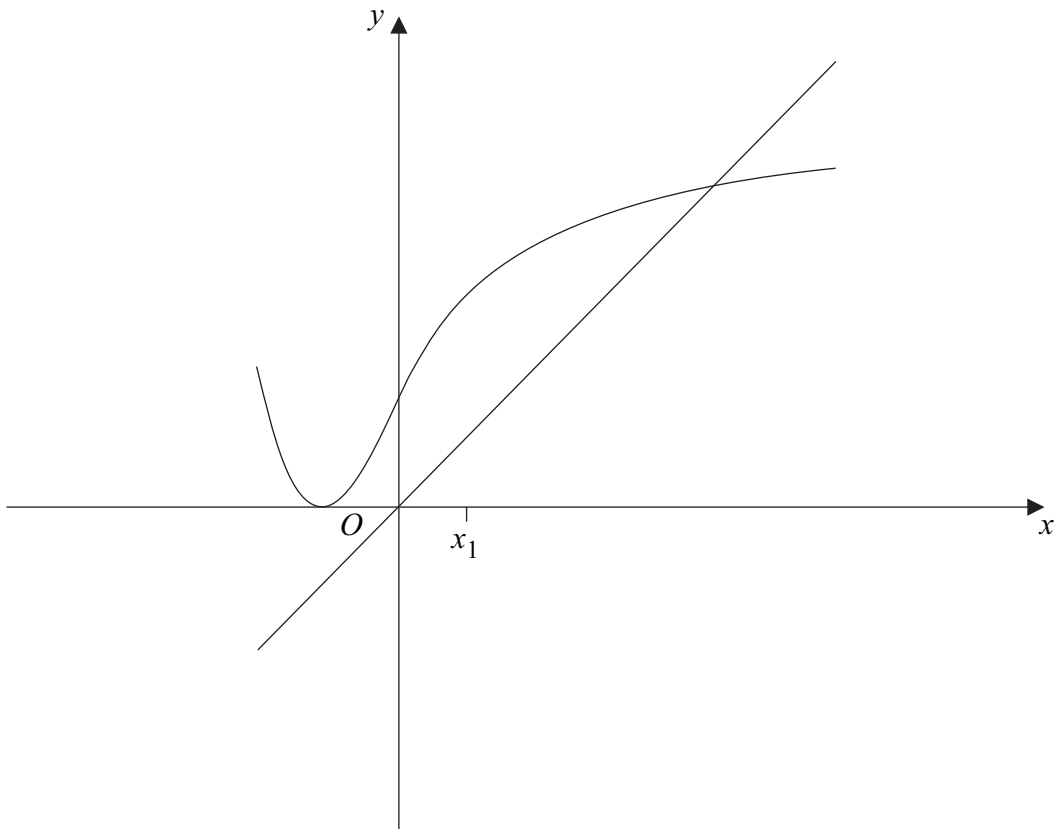
Turn over ►

QUESTION
PART
REFERENCE

Answer space for question 3

Area with horizontal dotted lines for writing the answer.

(c)



Turn over ►



QUESTION
PART
REFERENCE

Answer space for question 4

A large rectangular area with horizontal dotted lines for writing an answer.

Turn over ►



QUESTION
PART
REFERENCE

Answer space for question 5

A large rectangular area containing horizontal dotted lines for writing an answer.

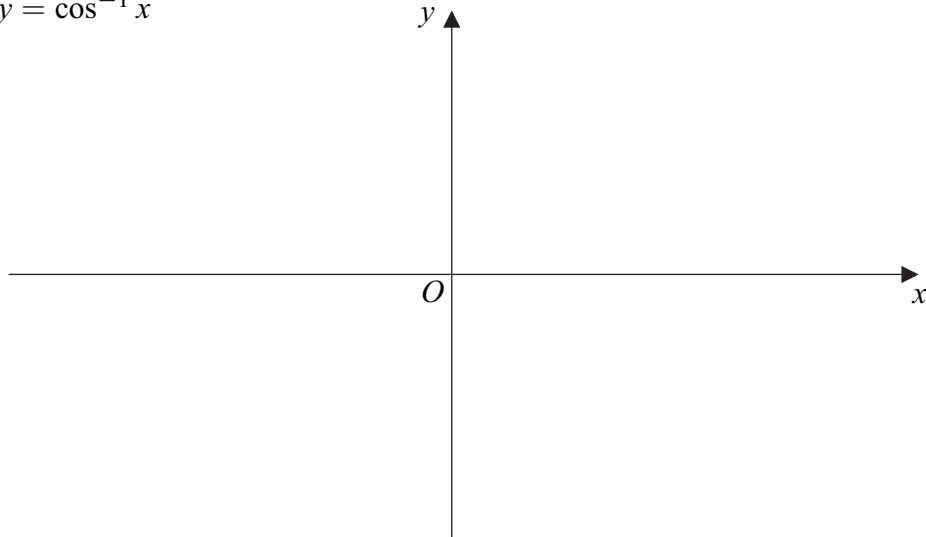
Turn over ►



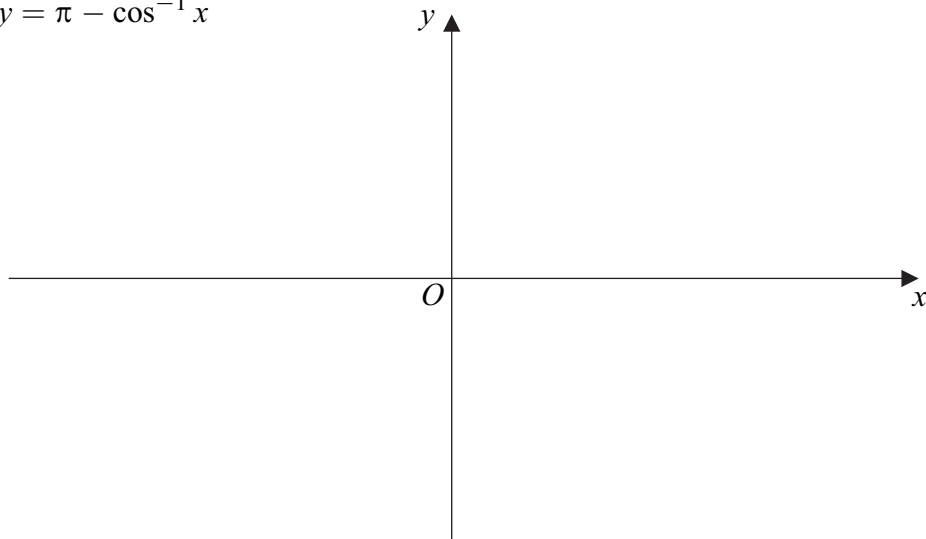
- 6 (a)** Sketch the graph of $y = \cos^{-1} x$, where y is in radians. State the coordinates of the end points of the graph. (2 marks)
- (b)** Sketch the graph of $y = \pi - \cos^{-1} x$, where y is in radians. State the coordinates of the end points of the graph. (2 marks)

QUESTION
PART
REFERENCE**Answer space for question 6****(a)**

$$y = \cos^{-1} x$$

**(b)**

$$y = \pi - \cos^{-1} x$$



QUESTION
PART
REFERENCE

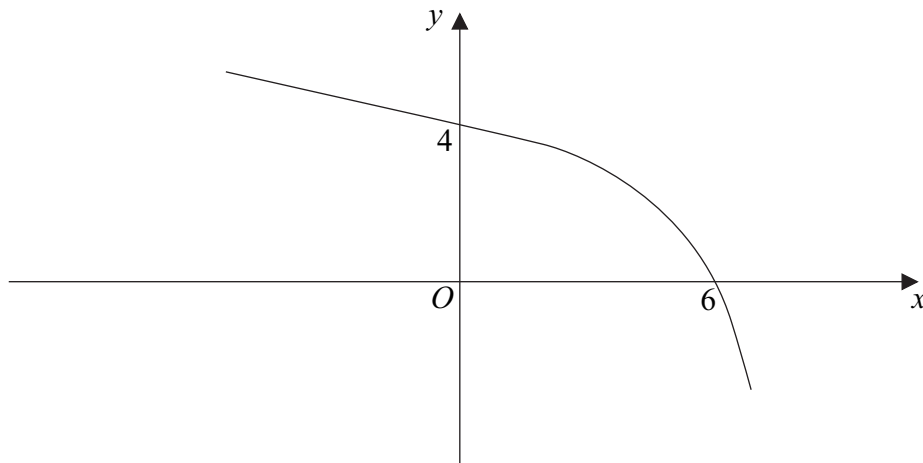
Answer space for question 6

A large rectangular area with horizontal dotted lines for writing an answer.

Turn over ►



- 7 The diagram shows a sketch of the curve with equation $y = f(x)$.



- (a) On **Figure 1**, below, sketch the curve with equation $y = -f(3x)$, indicating the values where the curve cuts the coordinate axes. (2 marks)
- (b) On **Figure 2**, on the opposite page, sketch the curve with equation $y = f(|x|)$, indicating the values where the curve cuts the coordinate axes. (3 marks)
- (c) Describe a sequence of two geometrical transformations that maps the graph of $y = f(x)$ onto the graph of $y = f\left(-\frac{1}{2}x\right)$. (4 marks)

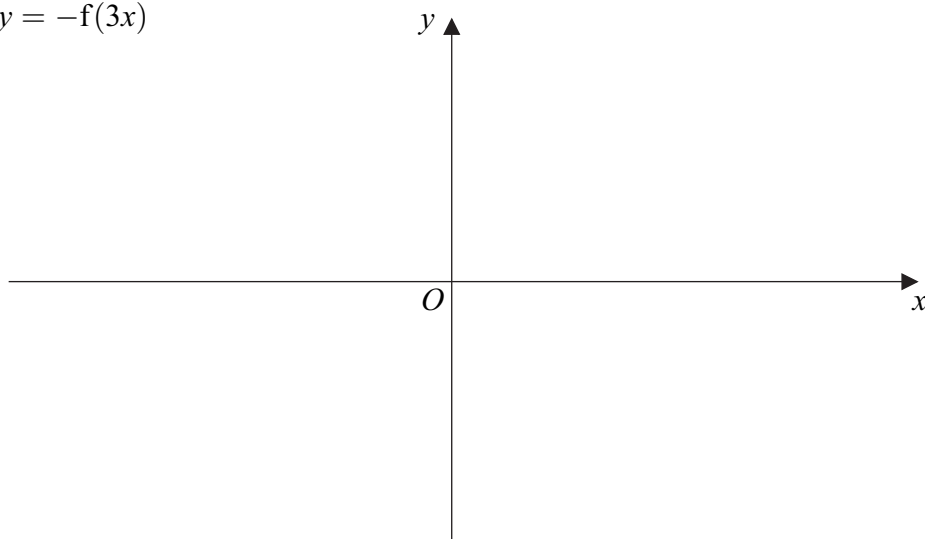
QUESTION
PART
REFERENCE

Answer space for question 7

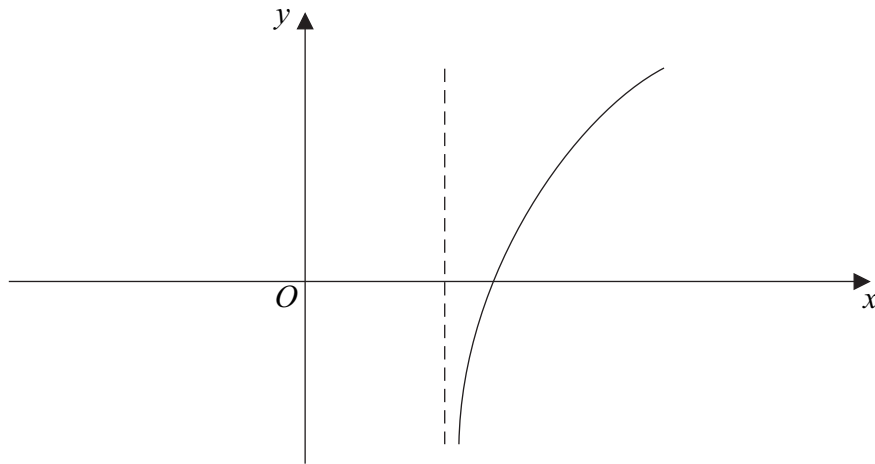
(a)

$$y = -f(3x)$$

Figure 1



- 8** The curve with equation $y = f(x)$, where $f(x) = \ln(2x - 3)$, $x > \frac{3}{2}$, is sketched below.



- (a)** The inverse of f is f^{-1} .
- (i)** Find $f^{-1}(x)$. *(3 marks)*
- (ii)** State the range of f^{-1} . *(1 mark)*
- (iii)** Sketch, on the axes given on the opposite page, the curve with equation $y = f^{-1}(x)$, indicating the value of the y -coordinate of the point where the curve intersects the y -axis. *(2 marks)*
- (b)** The function g is defined by
- $$g(x) = e^{2x} - 4, \text{ for all real values of } x$$
- (i)** Find $gf(x)$, giving your answer in the form $(ax - b)^2 - c$, where a , b and c are integers. *(3 marks)*
- (ii)** Write down an expression for $fg(x)$, and hence find the exact solution of the equation $fg(x) = \ln 5$. *(3 marks)*

QUESTION
PART
REFERENCE

Answer space for question 8

.....

.....

.....

.....

.....

.....

.....

.....



QUESTION
PART
REFERENCE

Answer space for question 8

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

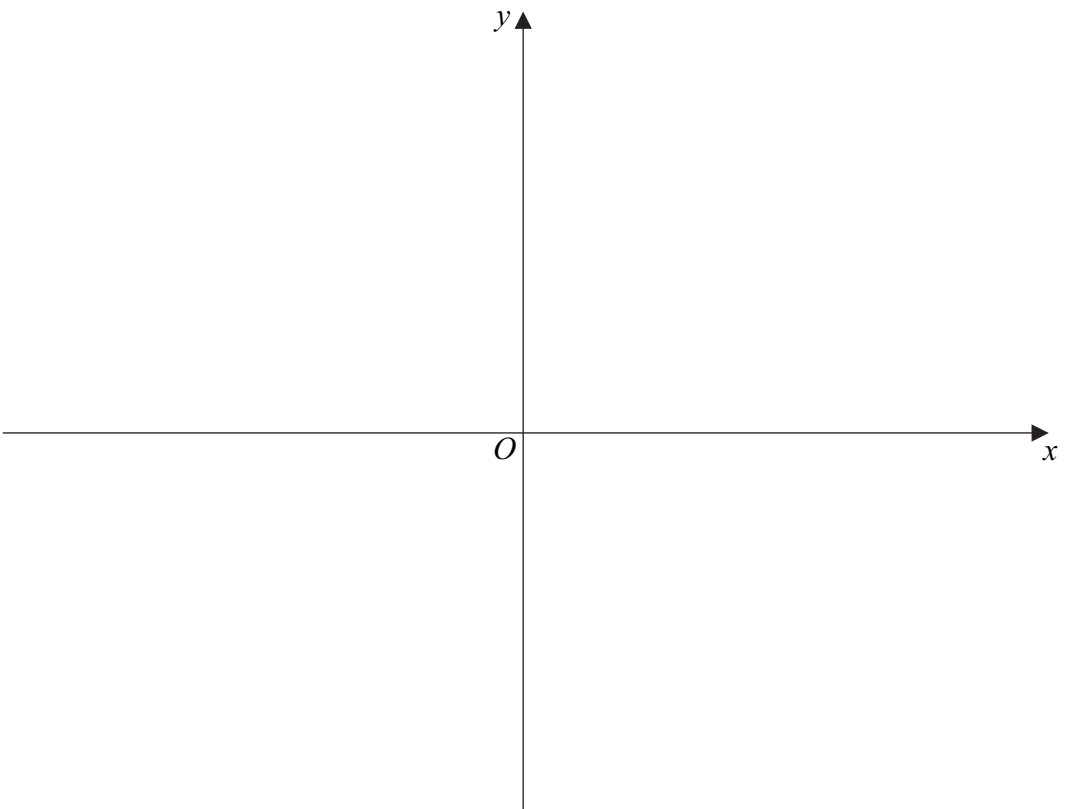
.....

.....

.....

.....

(a)(iii)



Turn over ►



QUESTION
PART
REFERENCE

Answer space for question 8

A large rectangular area with horizontal dotted lines for writing the answer to question 8.



QUESTION
PART
REFERENCE

Answer space for question 9

A large rectangular area with horizontal dotted lines for writing an answer.

Turn over ►



10 (a) (i) By writing $\ln x$ as $(\ln x) \times 1$, use integration by parts to find $\int \ln x \, dx$. (4 marks)

(ii) Find $\int (\ln x)^2 \, dx$. (4 marks)

(b) Use the substitution $u = \sqrt{x}$ to find the exact value of

$$\int_1^4 \frac{1}{x + \sqrt{x}} \, dx \quad (7 \text{ marks})$$

QUESTION
PART
REFERENCE

Answer space for question 10



QUESTION
PART
REFERENCE

Answer space for question 10

A large rectangular area with horizontal dotted lines for writing an answer.



