

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
TOTAL	



General Certificate of Education
Advanced Level Examination
June 2011

Mathematics

MS03

Unit Statistics 3

Wednesday 22 June 2011 9.00 am to 10.30 am

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The **final** answer to questions requiring the use of tables or calculators should normally be given to three significant figures.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.



J U N 1 1 M S 0 3 0 1

QUESTION
PART
REFERENCE

Turn over ►



0 5

- 3** An IT help desk has three telephone stations: Alpha, Beta and Gamma. Each of these stations deals only with telephone enquiries.

The probability that an enquiry is received at Alpha is 0.60.

The probability that an enquiry is received at Beta is 0.25.

The probability that an enquiry is received at Gamma is 0.15.

Each enquiry is resolved at the station that receives the enquiry. The **percentages** of enquiries resolved within various times at **each** station are shown in the table.

		Time		
		≤ 1 hour	≤ 24 hours	≤ 72 hours
Station	Alpha	55	80	100
	Beta	60	85	100
	Gamma	40	75	100

For example:

80 per cent of enquiries received at Alpha are resolved within 24 hours;

25 per cent of enquiries received at Alpha take between 1 hour and 24 hours to resolve.

- (a)** Find the probability that an enquiry, selected at random, is:
- (i)** resolved at Gamma; *(1 mark)*
 - (ii)** resolved at Alpha within 1 hour; *(1 mark)*
 - (iii)** resolved within 24 hours; *(2 marks)*
 - (iv)** received at Beta, given that it is resolved within 24 hours. *(3 marks)*
- (b)** A random sample of 3 enquiries was selected.
- Given that all 3 enquiries were resolved within 24 hours, calculate the probability that they were all received at:
- (i)** Beta; *(2 marks)*
 - (ii)** the same station. *(4 marks)*



5

An examination of 160 e-mails received by Gopal showed that 72 had attachments.

An examination of 250 e-mails received by Haley showed that 102 had attachments.

Stating **two** necessary assumptions about the selection of e-mails, construct an approximate 99% confidence interval for the difference between the proportion of e-mails received by Gopal that have attachments and the proportion of e-mails received by Haley that have attachments. *(8 marks)*

QUESTION
PART
REFERENCE

A series of horizontal dotted lines for writing the answer.



6 The weight, X grams, of a dressed pheasant may be modelled by a normal random variable with a mean of 1000 and a standard deviation of 120.

Pairs of dressed pheasants are selected for packing into boxes. The total weight of a pair, $Y = X_1 + X_2$ grams, may be modelled by a normal distribution with a mean of 2000 and a standard deviation of 140.

(a) (i) Show that $\text{Cov}(X_1, X_2) = -4600$. *(3 marks)*

(ii) Given that $X_1 - X_2$ may be assumed to be normally distributed, determine the probability that the difference between the weights of a selected pair of dressed pheasants exceeds 250 grams. *(5 marks)*

(b) The weight of a box is independent of the total weight of a pair of dressed pheasants, and is normally distributed with a mean of 500 grams and a standard deviation of 40 grams.

Determine the probability that a box containing a pair of dressed pheasants weighs less than 2750 grams. *(5 marks)*

QUESTION
PART
REFERENCE

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....



QUESTION
PART
REFERENCE

Lined writing area for student responses.

Turn over ►



7 (a) The random variable X has a Poisson distribution with $E(X) = \lambda$.

(i) Prove, from first principles, that $E(X(X - 1)) = \lambda^2$. *(3 marks)*

(ii) Hence deduce that $\text{Var}(X) = E(X)$. *(2 marks)*

(b) The random variable Y has a Poisson distribution with $E(Y) = 2.5$.

Given that $Z = 4Y + 30$:

(i) show that $\text{Var}(Z) = E(Z)$; *(3 marks)*

(ii) give a reason why the distribution of Z is **not** Poisson. *(1 mark)*

QUESTION
PART
REFERENCE

.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....



8 The tensile strength of rope is measured in kilograms.

The standard deviation of the tensile strength of a particular design of 10 mm diameter rope is known to be 285 kilograms. A retail organisation, which buys such rope from two manufacturers, A and B, wishes to compare their ropes for mean tensile strength.

The mean tensile strength, \bar{x} , of a random sample of 80 lengths from manufacturer A was 3770 kilograms.

The mean tensile strength, \bar{y} , of a random sample of 120 lengths from manufacturer B was 3695 kilograms.

- (a) (i)** Test, at the 5% level of significance, the hypothesis that there is no difference between the mean tensile strength of rope from manufacturer A and that of rope from manufacturer B. *(6 marks)*
- (ii)** Why was it **not** necessary to know the distributions of tensile strength in order for your test in part **(a)(i)** to be valid? *(1 mark)*
- (b) (i)** Deduce that, for your test in part **(a)(i)**, the critical values of $(\bar{x} - \bar{y})$ are ± 80.63 , correct to two decimal places. *(2 marks)*
- (ii)** In fact, the mean tensile strength of rope from manufacturer A exceeds that of rope from manufacturer B by 125 kilograms.

Determine the probability of a Type II error for a test of the hypothesis in part **(a)(i)** at the 5% level of significance, based upon a random sample of 80 lengths from manufacturer A and a random sample of 120 lengths from manufacturer B. *(4 marks)*

QUESTION
PART
REFERENCE

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....



QUESTION
PART
REFERENCE

A large rectangular area containing a grid of horizontal dashed lines for writing answers. The grid starts below the header and ends above the footer.

Turn over ►



QUESTION
PART
REFERENCE

Area with horizontal dotted lines for writing.

END OF QUESTIONS

Copyright © 2011 AQA and its licensors. All rights reserved.

