



General Certificate of Education
Advanced Subsidiary Examination
January 2010

Mathematics

MD01

Unit Decision 1

Tuesday 19 January 2010 9.00 am to 10.30 am

For this paper you must have:

- an 8-page answer book
- the blue AQA booklet of formulae and statistical tables
- an insert for use in Questions 3 and 7 (enclosed).

You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil or coloured pencil should only be used for drawing.
- Write the information required on the front of your answer book. The **Examining Body** for this paper is AQA. The **Paper Reference** is MD01.
- Answer **all** questions.
- Show all necessary working; otherwise marks for method may be lost.
- The **final** answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.
- Fill in the boxes at the top of the insert.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Answer **all** questions.

- 1 Six girls, Alfonsa (A), Bianca (B), Claudia (C), Desiree (D), Erika (E) and Flavia (F), are going to a pizza restaurant. The restaurant provides a special menu of six different pizzas: Margherita (M), Neapolitana (N), Pepperoni (P), Romana (R), Stagioni (S) and Viennese (V).

The table shows the pizzas that each girl likes.

Girl	Pizza
Alfonsa (A)	Margherita (M), Pepperoni (P), Stagioni (S)
Bianca (B)	Neapolitana (N), Romana (R)
Claudia (C)	Neapolitana (N), Viennese (V)
Desiree (D)	Romana (R), Stagioni (S)
Erika (E)	Pepperoni (P), Stagioni (S), Viennese (V)
Flavia (F)	Romana (R)

- (a) Show this information on a bipartite graph. (2 marks)
- (b) Each girl is to eat a different pizza. Initially, the waiter brings six different pizzas and gives Alfonsa the Pepperoni, Bianca the Romana, Claudia the Neapolitana and Erika the Stagioni. The other two pizzas are put in the middle of the table.

From this initial matching, use the maximum matching algorithm to obtain a complete matching so that every girl gets a pizza that she likes. List your complete matching.

(5 marks)

- 2 (a) Use a bubble sort to rearrange the following numbers into ascending order.

13 16 10 11 4 12 6 7 (5 marks)

- (b) State the number of comparisons and the number of swaps (exchanges) for each of the first three passes. (3 marks)

- 3 [Figure 1, printed on the insert, is provided for use in this question.]

The feasible region of a linear programming problem is represented by the following:

$$x \geq 0, y \geq 0$$

$$x + 4y \leq 36$$

$$4x + y \leq 68$$

$$y \leq 2x$$

$$y \geq \frac{1}{4}x$$

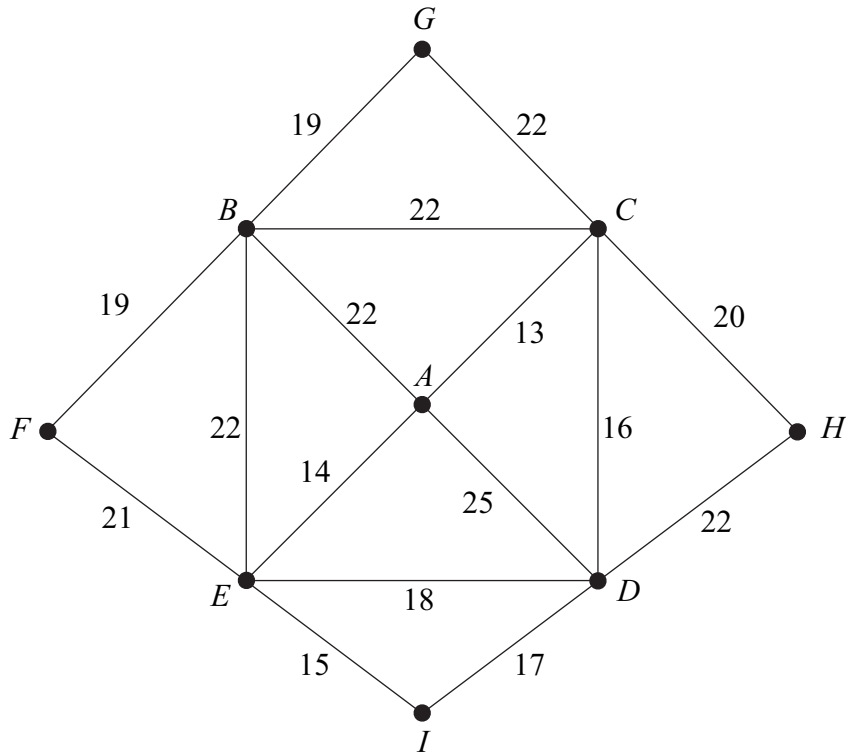
- (a) On **Figure 1**, draw a suitable diagram to represent the inequalities and indicate the feasible region. (6 marks)
- (b) Use your diagram to find the maximum value of P , stating the corresponding coordinates, on the feasible region, in the case where:
- (i) $P = x + 5y$; (2 marks)
- (ii) $P = 5x + y$. (2 marks)

Turn over for the next question

Turn over ►

- 4 In Paris, there is a park where there are statues of famous people; there are many visitors each day to this park. Lighting is to be installed at nine places, A, B, \dots, I , in the park. The places have to be connected either directly or indirectly by cabling, to be laid alongside the paths, as shown in the diagram.

The diagram shows the length of each path, in metres, connecting adjacent places.



Total length of paths = 307 metres

- (a) (i) Use Prim's algorithm, starting from A , to find the minimum length of cabling required. (5 marks)
- (ii) State this minimum length. (1 mark)
- (iii) Draw the minimum spanning tree. (2 marks)
- (b) A security guard walks along all the paths before returning to his starting place. Find the length of an optimal Chinese postman route for the guard. (6 marks)

- 5 There is a one-way system in Manchester. Mia is parked at her base, B , in Manchester and intends to visit four other places, A , C , D and E , before returning to her base. The following table shows the distances, in kilometres, for Mia to drive between the five places A , B , C , D and E . Mia wants to keep the total distance that she drives to a minimum.

From \ To	A	B	C	D	E
A	–	1.7	1.9	1.8	2.1
B	3.1	–	2.5	1.8	3.7
C	3.1	2.9	–	2.7	4.2
D	2.0	2.8	2.1	–	2.3
E	2.2	3.6	1.9	1.7	–

- (a) Find the length of the tour $BECDAB$. (1 mark)
- (b) Find the length of the tour obtained by using the nearest neighbour algorithm starting from B . (4 marks)
- (c) Write down which of your answers to parts (a) and (b) would be the better upper bound for the total distance that Mia drives. (1 mark)
- (d) On a particular day, the council decides to reverse the one-way system. For this day, find the length of the tour obtained by using the nearest neighbour algorithm starting from B . (4 marks)

Turn over for the next question

Turn over ►

6 A student is finding a numerical approximation for the area under a curve.

The algorithm that the student is using is as follows:

```
Line 10      Input  $A, B, N$ 
Line 20      Let  $T = 0$ 
Line 30      Let  $D = A$ 
Line 40      Let  $H = (B - A)/N$ 
Line 50      Let  $E = H/2$ 
Line 60      Let  $T = T + A^3 + B^3$ 
Line 70      Let  $D = D + H$ 
Line 80      If  $D = B$  then go to line 110
Line 90      Let  $T = T + 2D^3$ 
Line 100     Go to line 70
Line 110     Print 'Area = ',  $T \times E$ 
Line 120     End
```

Trace the algorithm in the case where the input values are:

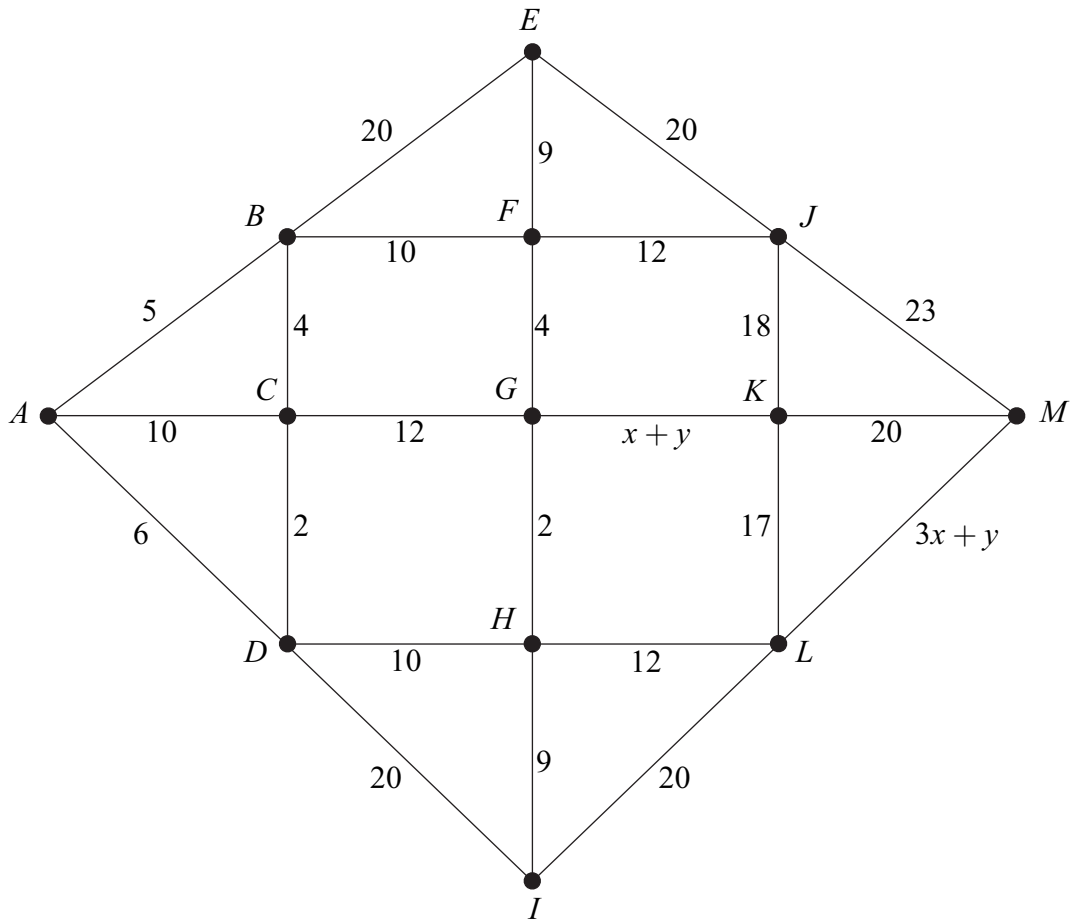
(a) $A = 1, B = 5, N = 2;$ (4 marks)

(b) $A = 1, B = 5, N = 4.$ (4 marks)

7 [Figure 2, printed on the insert, is provided for use in this question.]

The following network has 13 vertices and 24 edges connecting some pairs of vertices. The number on each edge is its weight.

The weights on the edges GK and LM are functions of x and y , where $x > 0$, $y > 0$ and $10 < x + y < 27$.



There are three routes from A to M of the same minimum total weight.

- (a) Use Dijkstra's algorithm on **Figure 2** to find this minimum total weight. (7 marks)
- (b) Find the values of x and y . (3 marks)

Turn over for the next question

Turn over ►

- 8 A factory packs three different kinds of novelty box: red, blue and green. Each box contains three different types of toy: A, B and C.

Each red box has 2 type A toys, 3 type B toys and 4 type C toys.

Each blue box has 3 type A toys, 1 type B toy and 3 type C toys.

Each green box has 4 type A toys, 5 type B toys and 2 type C toys.

Each day, the maximum number of each type of toy available to be packed is 360 type A, 300 type B and 400 type C.

Each day, the factory must pack more type A toys than type B toys.

Each day, the total number of type A and type B toys that are packed must together be at least as many as the number of type C toys that are packed.

Each day, at least 40% of the total toys that are packed must be type C toys.

Each day, the factory packs x red boxes, y blue boxes and z green boxes.

Formulate the above situation as 6 inequalities, in addition to $x \geq 0$, $y \geq 0$ and $z \geq 0$, simplifying your answers. *(8 marks)*

END OF QUESTIONS