

Student Bounty.com

Dulwich College

SPECIMEN UPPER SCHOOL ENTRANCE EXAMINATION

MATHEMATICS 1 HOUR 30 MINUTES

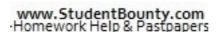
Note: The questions in this specimen paper are designed to give an idea of the <u>style</u> of question which will be tested. The exact content of the entrance paper you will sit will not necessarily be the same.

Use a calculator where appropriate.

Attempt all the questions.

Show all your working.

Surname:	Date:
First Name:	Present School:
Age:	Mathematics Qualifications Achieved So Far:



Formulae

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Quadratic Equation:
$$ax^2 + bx + c = 0, a \ne 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Sine Rule:
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Cosine Rule:
$$a^2 = b^2 + c^2 - 2bc \cos A$$
 or

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

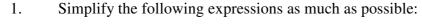
Volumes: Cone:
$$\frac{1}{3}\pi r^2 h$$

Cylinder:
$$\pi r^2 h$$

Sphere: $\frac{4}{3} \pi r^3$

Section A

StudentBounts.com The questions in this section test standard algebra (such as factorising, indices, solving equations, completing the square, algebraic manipulation), coordinate geometry & trigonometry



(i)
$$\frac{5x + 25}{10x - 20}$$

Answer: _____

(ii)
$$\frac{2x^2 + 2x - 12}{x^2 - x - 12}$$

Answer: _____

(iii)
$$\frac{x^3 - x^2}{x - 1}$$

Answer: _____

2. Find the equation of the straight line through (2, -4) and (-9, 7), writing your answer in the form y = mx + c.

Answer: _____

(i) $\sin x = \sin 50^{\circ}$

Answer: _____

(ii) $\cos 2x = -\frac{\sqrt{3}}{2}$

Answer: *x* =_____

5.(a) Express each of the following as a power of 2 (i.e. in the form 2^x):

(i)

Answer: _____

(ii)

Answer:

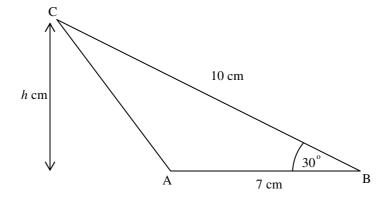
(iii)

Answer: _____

 $25^{3x} = \frac{1}{625}.$ Solve the equation for *x*: (b)

Answer: _____

6. In triangle ABC shown below (not drawn to scale), AB = 7 cm, BC = 10 and angle ABC = 30° . The perpendicular height of the triangle is h cm



Giving your answers to 3 significant figures where appropriate, calculate the:

(i) length AC;

(ii) area of triangle ABC;

(iii) perpendicular height, h, of the triangle as shown in the diagram.

Answer: $h = \underline{\hspace{1cm}} cm$

P. PRINTER COM Solve the following equation for *x*, giving your answers to 1 decimal place: 7.

$$\frac{2}{x-1} - \frac{3}{x+1} = 4$$

Answer:			

Section B

SHILDER BOUNTS, COM The questions in this section are more stretching than those in section A and even though you may not have seen questions like these before they can all be answered with a little thought.

Simplify the following $\frac{4}{x-3} + \frac{3x-3}{(x^2-x-6)}$ expressing your answer as a single 1.(i) fraction.

Answer: _____

(ii) Hence solve
$$\frac{4}{x-3} + \frac{3x-3}{(x^2-x-6)} = \frac{2-20x}{2x+4}$$

Answer: _____

3. Solve the simultaneous equations:

$$x - 2y = 1$$

$$x - 2y = 1$$
$$x^2 - xy + y^2 = 1$$

Answer:

Use this to solve: $\sin x + \cos x = 0$, for all x where $0^{\circ} \le x \le 180^{\circ}$.

Answer: *x* =_____ °

- 5. You are given that $x^3 2x^2 25x + 50 = (x-2)(ax^2 + bx + c)$ where a, b and c are integers.
- (i) Write down the values of a, c.

Answer: *a* = _____ *c* = _____

(ii) Calculate the value of b.

Answer: *b* =_____

(iii) Hence solve the equation $x^3 - 2x^2 - 25x + 50 = 0$.

Answer: *x* =_____

6. You are given that $(x + y)^5 = x^5 + 5x^4y + 10x^3y^2 + 10x^2y^3 + 5xy^4 + y^5$ Use this to expand the brackets and then simplify your answers in:

(i)
$$(1-y)^5$$

Answer:
$$(1 - y)^5 =$$

(ii)
$$(2x - y)^5$$

Answer:
$$(2x - y)^5 =$$

(iii)
$$(x - \sqrt{2})^5 (x + \sqrt{2})^5$$

Answer:
$$(x - \sqrt{2})^5 (x + \sqrt{2})^5 =$$

Section C

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1. Find
$$\frac{dy}{dx}$$
:

(i)
$$y = 5x^4 - x - 2$$
,

Answer:
$$\frac{dy}{dx} =$$

(ii)
$$y = \frac{1}{\sqrt{x}}$$
,

Answer:
$$\frac{dy}{dx} =$$

2.(i) Find
$$\int x^3 (x-4) dx$$

(ii) Evaluate
$$\int_{0}^{1} \left(\frac{x^{3} + x^{2}}{x^{2}} \right) dx$$

Answer: _____

END OF EXAMINATION